

## Full Articles

### Molecular modeling of hydration properties of hydrophobic ions $\text{Li}^+@C_{60}$ and $\text{K}^+@C_{60}$

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The Gibbs free energies of solvation ( $\Delta G_s$ ) and the electronic structures of endohedral metallofullerenes  $M^+@C_{60}$  ( $M^+ = \text{Li}^+, \text{K}^+$ ) were calculated within the framework of the density functional theory and the polarizable continuum model. In water environment, the equilibrium position of  $\text{K}^+$  is at the center of the fullerene cavity whereas that of  $\text{Li}^+$  is shifted by 0.14 nm toward the fullerene cage. The  $\text{Li}^+$  cation is stabilized by interactions with both the fullerene and solvent. The equilibrium structures of both endohedral metallofullerenes are characterized by very close  $\Delta G_s$  values. In particular, the calculated  $\Delta G_s$  values for  $\text{K}^+@C_{60}$  are in the range from  $-124$  to  $-149 \text{ kJ mol}^{-1}$  depending on the basis set and on the type of the density functional. Molecular dynamics simulations (TIP3P  $\text{H}_2\text{O}$ , OPLS force field, water sphere of radius 1.9 nm) showed that the radial distribution functions of water density around  $C_{60}$  and  $M^+@C_{60}$  are very similar, whereas orientations of water dipoles around the endohedral metallofullerenes resemble the hydration pattern of isolated metal ions.

**Key words:** fullerene, endohedral metallofullerene, the Gibbs free energy of solvation, density functional theory, polarizable continuum model, molecular dynamics, the Langevin dipoles.

Fullerene derivatives are a new interesting class of synthetic biologically active compounds (BACs). Relatively large size, regular spherical shape, and great potential of chemical modification make fullerenes, in particular,  $C_{60}$ , promising pharmacophore constituents of BACs.<sup>1–5</sup> Specific features of the molecular structure of fullerenes suggest that proteins and other natural biomolecules may contain fullerene-specific binding sites. In this connection, quantitative description of the effect of the fullerene frag-

ment on the physicochemical properties of fullerene-containing compounds becomes of great importance. This first of all concerns studies of the interactions between fullerenes and their environment in biological media. Fullerenes are poorly soluble in polar solvents, show a somewhat better solubility in nonpolar aliphatic hydrocarbons, being well soluble only in aromatic hydrocarbons.<sup>6–9</sup> They are highly hydrophobic, readily stick to one another, and have an extremely low (not determined ex-

perimentally) solubility in water.<sup>7</sup> Nevertheless, fullerene derivatives containing polar groups can be dissolved in water with ease.<sup>4,5</sup>

A possible method for increasing the solubility of fullerene-containing compounds in aqueous media is the introduction of metal ions into the fullerene cage. Charged endohedral metallofullerenes can be treated as bulk hydrophobic ions. In some cases, the functional group of a charged endohedral metallofullerene can have different, as compared to the electrically neutral fullerene, binding sites to biomolecules.

The structure and dynamics of the hydration shells surrounding hydrophobic fullerene nanomolecules are also of interest from the standpoint of basic research. Until recently, ionic forms of endohedral metallofullerenes were unknown and could be treated only as hypothetical structures. However, a recently reported<sup>10</sup> synthesis and structural characterization of endohedral metallofullerene  $\text{Li}^+@C_{60}$  likely suggests that other compounds belonging to this class can be synthesized.

The aim of the present study was to investigate the thermodynamics and structural aspects of the interactions of two endohedral metallofullerenes  $\text{M}^+@C_{60}$  ( $\text{M}^+ = \text{Li}^+, \text{K}^+$ ) with water environment by computational chemistry methods. Monatomic lithium and potassium cations were chosen as important representatives of Group I alkali metals. Experiments showed that a relatively small lithium ion encapsulated in the fullerene  $C_{60}$  cage can move within about 0.3 nm.<sup>10</sup> The distance allowed for the larger potassium ion to move within the  $C_{60}$  sphere seems to be shorter. In the present work, we calculated the Gibbs free energies of solvation ( $\Delta G_s$ ) of the title hydrophobic ions in water. By definition,  $\Delta G_s$  is the Gibbs free energy of transfer of a compound from the gas phase to a solution (see, e.g., Ref. 11). To date, the experimental  $\Delta G_s$  values for water have not been determined for all known fullerenes. In the present work, the  $\Delta G_s$  values were estimated within the framework of the density functional theory (DFT) and the polarizable continuum model (PCM). Also, the molecular dynamics (MD) simulations for microscopic models for the hydrated metallofullerenes  $\text{M}^+@C_{60}$  were carried out. Some problems in research on the physicochemical properties of fullerenes in solution were investigated earlier by both DFT<sup>12–14</sup> and MD methods.<sup>15–20</sup>

### Calculation Procedure

The Gibbs free energies of solvation of  $\text{M}^+@C_{60}$  were calculated within the framework of the DFT and the PCM model using the Gaussian-03 program.<sup>21</sup> The solvation model used is based on representation of the solvent by a continuous polarizable medium in which the solute molecule forms a cavity with a well-defined boundary. The standard Gibbs free energy of sol-

vation  $\Delta G_s$  is calculated in the PCM as the sum of the following contributions

$$\Delta G_s = \Delta G_{\text{el}} + \Delta G_{\text{cav}} + \Delta G_{\text{disp}} + \Delta G_{\text{rep}},$$

where  $\Delta G_{\text{el}}$  is the energy of electrostatic interaction of solute molecules with the dielectric continuum (including their mutual polarization),  $\Delta G_{\text{cav}}$  is the Gibbs free energy of formation of a cavity in the dielectric medium,  $\Delta G_{\text{disp}}$  is the energy of dispersion interaction, and  $\Delta G_{\text{rep}}$  is the electron-electron repulsion energy.<sup>22–24</sup> The universal force field<sup>21</sup> (UFF) parameterization of atomic radii was used. In constructing the solvent cavity the molecular surfaces were augmented with (i) a sphere of radius 0.324 nm inscribed into the  $C_{60}$  cage and centered at the center of the fullerene molecule and (ii) spherical fragments to smooth the outer surface of the molecule (the last-mentioned procedure is by default used in the Gaussian-03 program).<sup>21</sup> The fullerene wave functions were calculated in the 6-31G(d), 6-31+G(d), and LANL2DZ basis sets<sup>21,25</sup> (LANL2DZ is the basis set optimized for the alkali metal calculations). The results obtained with a number of DFT computational schemes using various exchange and correlation functionals were analyzed. Three-dimensional structures of endohedral metallofullerenes were constructed based on the experimental data for  $C_{60}$  thiophene disolvate<sup>26</sup> (localization of the alkali metal ion was studied additionally).

MD calculations were performed for the fullerenes located at the center of a water sphere of radius 1.9 nm comprising 922 water molecules. Potential energy calculations were carried out using the OPLS force field;<sup>27</sup> the potentials of nonbonding site—site interactions were specified as follows:

$$U(r_{ij}) = 4\epsilon_{ij}[(\sigma_{ij}/r_{ij})^{12} - (\sigma_{ij}/r_{ij})^6] + q_i q_j / r_{ij},$$

where  $i$  and  $j$  enumerate atoms belonging to different molecules, and included contributions from the dispersion and Coulomb interactions and the electron—electron repulsion energies. In particular, the Lennard-Jones parameters of aromatic carbon atoms ( $\sigma_i = 0.355$  nm,  $\epsilon_i = 0.070$  kJ mol<sup>−1</sup>) were used for  $C_{60}$ . The atomic charges  $q_i$  were estimated from DFT calculations; for  $\text{K}^+@C_{60}$ , they are 0.880 on K and 0.002 on C. The 6—5 and 6—6 bond lengths in the  $C_{60}$  molecule were set equal to 0.1385 and 0.1451 nm, respectively, taking into account the X-ray data.<sup>26</sup> The TIP3P parameters ( $\sigma_i(\text{O}) = 0.315$  nm,  $\epsilon_i(\text{O}) = 0.636$  kJ mol<sup>−1</sup>,  $q_i(\text{O}) = -0.834$ )<sup>28</sup> were used for water molecules; the cations parameters taken from Ref. 29 were as follows:  $\sigma_i = 0.213$  nm,  $\epsilon_i = 0.076$  kJ mol<sup>−1</sup> for  $\text{Li}^+$  and  $\sigma_i = 0.494$  nm,  $\epsilon_i = 0.001$  kJ mol<sup>−1</sup> for  $\text{K}^+$ . Molecular simulation was carried out using a localized parallel version of an MD program.<sup>30</sup> The SCAAS spherical boundary conditions<sup>31</sup> were taken into account for the water drop. Water molecules and fullerene were considered rigid within the SHAKE algorithm.<sup>32</sup> The fullerene carbon atoms were restrained with a harmonic potential to hold them together within a sphere of radius 0.37 nm (if the distance from a given C atom to the center of the system was shorter than 0.37 nm, the restraining potential was set equal to zero; at distances longer than 0.37 nm, the atom was in a harmonic potential with a constant of 20.9 kJ mol<sup>−1</sup>). MD calculations were performed for  $T = 300$  K using a thermostat relaxation time  $\tau_T = 0.2$  ps and a time step of 2 fs. In calculations of the radial distribution functions (RDF) the model systems were equilibrated over a period of 5 ns, followed by a 2 ns MD simulation after each five

steps on the MD trajectory. The RDF for the orientation of water dipoles

$$f_{\theta}(r) \equiv \langle \cos(\theta) \rangle = \langle (\vec{\mu}_w / r_w) \rangle / (\mu_w / r_w)$$

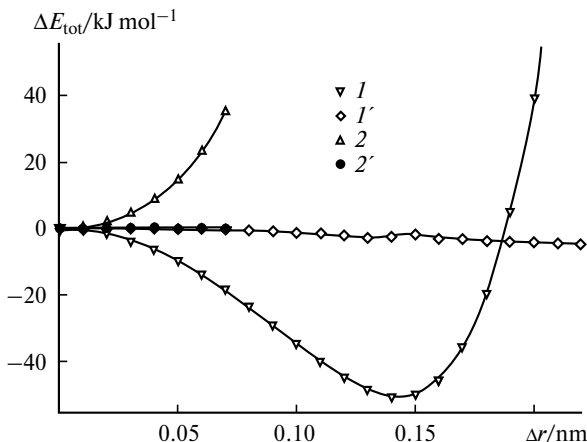
were calculated taking into account the histograms of the cosine of the orientation angle of the water dipole vector  $\vec{\mu}_w$  in the corresponding spherical layer of the solvent. The radius-vector  $\vec{r}_w$  of the center of a point water dipole was calculated by a rigorous expression

$$\vec{r}_w = \vec{r}_O/2 + \vec{r}_{H(1)}/4 + \vec{r}_{H(2)}/4.$$

The radius of the spherical cells for constructing the RDF histograms was 0.005 nm.

## Results and Discussion

In studies of the structures of charged endohedral metallofullerenes, an important issue is location of the metal ion within the fullerene cage. The results of B3LYP/LANL2DZ calculations of the energy characteristics of the motion of the  $\text{Li}^+$  and  $\text{K}^+$  ions from the center of the fullerene sphere toward the center of a hexagon carried out with inclusion of the solvent effect are shown in Fig. 1. The ion motion coordinate was chosen based on experimental data.<sup>10</sup> According to calculations, transition of  $\text{M}^+@C_{60}$  from the gas phase to the aqueous medium is exothermic (see also Table 1). From the plots in Fig. 1 it also follows that the total energy ( $E_{\text{tot}}$ ) minimum for  $\text{Li}^+@C_{60}$  in the gas phase is attained at a distance  $\Delta r_{\text{min}} \approx 0.14$  nm from the center. Displacement of  $\text{Li}^+$  to the outermost position relative to the center causes  $\Delta G_s(\text{Li}^+@C_{60})$  to decrease by about 5 kJ mol<sup>-1</sup>. Thus,  $\text{Li}^+$  displaced from the center toward the inner surface of  $C_{60}$  fullerene is stabilized by both intramolecular interactions and interactions with water. For  $\text{K}^+@C_{60}$ , the minimum of  $E_{\text{tot}}$  corresponds to  $\Delta r_{\text{min}} = 0$ . In the range of allowed  $\Delta r$  values, changes in  $\Delta G_s$  for  $\text{K}^+$  are small, being at most 0.1 kJ mol<sup>-1</sup>. Consideration of the total energies in solution causes no changes in position of the total energy minimum compared to the gas-phase case. The equilibrium  $\Delta r_{\text{min}}$  values for both endohedral metallofullerenes also remain unchanged when using the B3PW91 instead of B3LYP functional. The results of calculations are in good agreement with the experimental position of the  $\text{Li}^+$  ion ( $\Delta r_{\text{min}} = 0.134$  nm) in the  $\text{Li}^+@C_{60}$  complex with the  $\text{SbCl}_6^-$  counterion.<sup>10</sup> By and large, the positions of the minima in Fig. 1 are in qualitative agreement with the radii of the ions in question. For instance, the van der Waals parameters  $\sigma_{ij}$  of the interactions between  $\text{K}^+$  and C atoms are 0.068 nm larger than the average distance  $\langle r(\text{center}-\text{C}) \rangle = 0.351$  nm from the C atoms to the center of the  $C_{60}$  sphere; this suggests localization of the ions at the center of the fullerene cage. Contrary to this, the  $\sigma_{ij}$  parameters for  $\text{Li}^+$  and C atoms is 0.076 nm smaller than  $\langle r(\text{center}-\text{C}) \rangle$ .



**Fig. 1.** Total energies ( $\Delta E_{\text{tot}}$ ) plotted vs. displacement ( $\Delta r$ ) of the ion from the center of the fullerene cage along a straight line to the center of a hexagon: changes in the total energies of isolated  $\text{Li}^+@C_{60}$  (1) and  $\text{K}^+@C_{60}$  (2), electrostatic contribution to the relative energies of hydration  $\text{Li}^+@C_{60}$  (1') and  $\text{K}^+@C_{60}$  (2'). Obtained from B3LYP/LANL2DZ/PCM calculations.

The results of calculations of the Gibbs free energies of solvation  $\Delta G_s(\text{M}^+@C_{60})$  are listed in Tables 1 and 2. The data in Table 1 characterize how the changes in the basis set and in the shape of the potential affect the energy characteristics of  $\text{K}^+@C_{60}$  with rigid geometry. The  $\Delta G_s(\text{K}^+@C_{60})$  values lie between  $-124$  and  $-149$  kJ mol<sup>-1</sup>. A comparison of the results obtained using three basis sets (see Table 1) shows that the smallest negative  $\Delta G_s$  values were obtained in calculations with the 6-31G(d) basis set. Augmentation with diffuse functions on going from the 6-31G(d) to the 6-31+G(d) basis set causes  $\Delta G_s$  to become more negative (by 5–10 kJ mol<sup>-1</sup>). The  $\Delta G_s$  values obtained from calculations with the LANL2DZ basis set are even more negative (by 1–10 kJ mol<sup>-1</sup>). The  $\Delta G_s$  values obtained using different density functionals and the same basis set differ insignificantly, whereas the Hartree–Fock calculations give the largest negative values in all cases. Note that calculations by all methods predict positive  $\Delta G_s$  values for the fullerene  $C_{60}$ , e.g.,  $\Delta G_s(C_{60}) = 14.8$  kJ mol<sup>-1</sup> according to B3PW91/LANL2DZ calculations.

The contributions to  $\Delta G_s$  calculated for the endohedral metallofullerenes by the B3LYP/LANL2DZ method using the equilibrium  $\Delta r_{\text{min}}$  values are listed in Table 2. The net nonpolar contributions for  $\text{Li}^+@C_{60}$  and  $\text{K}^+@C_{60}$  are  $+24.2$  and  $+22.4$  kJ mol<sup>-1</sup>, respectively, thus being small compared to the energy of electrostatic interactions. The total value of  $\Delta G_s(\text{Li}^+@C_{60})$  is  $-137.9$  kJ mol<sup>-1</sup>, which is very close to  $\Delta G_s(\text{K}^+@C_{60}) = -137.5$  kJ mol<sup>-1</sup>. The  $\Delta G_{\text{el}}$  and  $\Delta G_s$  values calculated by the B3LYP/LANL2DZ method for the ions located at the center of the cage ( $\Delta r = 0$ ) are respectively  $-159.7$  and  $-159.9$  kJ mol<sup>-1</sup> for  $\text{Li}^+@C_{60}$  and  $-135.4$  and  $-137.5$  kJ mol<sup>-1</sup> for  $\text{K}^+@C_{60}$ . The difference  $\Delta G_s = 2.1$  kJ mol<sup>-1</sup> is mainly due to the contribution of

**Table 1.** The Gibbs free energies of solvation ( $\Delta G_s/\text{kJ mol}^{-1}$ ) and the electron charges ( $q/e$ ) of  $\text{K}^+\text{@C}_{60}$ <sup>a</sup> calculated by different methods using the 6-31G(d), G-31+(d), and LANL2DZ basis sets

Computational method	6-31G(d)			6-31+G(d)			LANL2DZ		
	$-\Delta G_s^b$	$q_K(\text{Mull})^c$	$q_K(\text{NAO})^c$	$-\Delta G_s$	$q_K(\text{Mull})$	$q_K(\text{NAO})$	$-\Delta G_s$	$q_K(\text{Mull})$	$q_K(\text{NAO})$
HF <sup>d</sup>	131.2	0.99	0.92	139.6	1.15	0.87	149.2	1.02	0.88
SWVNe	123.7	0.79	0.90	130.7	0.49	0.87	134.2	0.81	0.90
OPBE <sup>e</sup>	124.1	1.16	0.91	128.9	1.56	0.86	133.2	1.14	0.89
OLYP <sup>e</sup>	124.7	1.02	0.92	132.8	1.29	0.86	134.6	1.00	0.89
BLYP <sup>e</sup>	125.2	0.76	0.91	135.0	0.48	0.87	135.8	0.76	0.90
B3LYP <sup>e</sup>	125.9	0.83	0.91	134.5	0.61	0.87	137.5	0.83	0.90
B3PW91 <sup>e</sup>	125.4	0.93	0.91	131.3	0.77	0.87	136.2	0.92	0.89

<sup>a</sup> Calculations for  $\Delta r_{\min}(\text{K}^+)$ .<sup>b</sup> The sum of nonpolar contributions to  $\Delta G_s$  is 22.4 kJ mol<sup>-1</sup>.<sup>c</sup>  $q_K(\text{Mull})$  and  $q_K(\text{NAO})$  are the electron density on  $\text{K}^+$  calculated according to Mulliken and for the natural orbitals, respectively.<sup>d</sup> Hartree–Fock calculations.<sup>e</sup> Density functional.<sup>20</sup>

dispersion interaction. As mentioned above, displacement of the  $\text{Li}^+$  ion from the center of the cage toward the equilibrium position causes  $\Delta G_s(\text{Li}^+\text{@C}_{60})$  to be close to  $\Delta G_s(\text{K}^+\text{@C}_{60})$ . Thus, the data in Tables 1 and 2 show that, in spite of different positions of the alkali metal ions within the fullerene cage,  $\text{Li}^+\text{@C}_{60}$  and  $\text{K}^+\text{@C}_{60}$  are stabilized in a similar manner in water environment. This is in high contrast with the difference between the experimental  $\Delta G_s$  values for these ions in water, *viz.*,  $-476$  and  $-511$  kJ mol<sup>-1</sup> (see Refs 33 and 29, respectively) for  $\text{Li}^+$  and  $-298$  and  $-337$  kJ mol<sup>-1</sup> (see Refs 33 and 29, respectively) for  $\text{K}^+$ . The experimental values of the Gibbs free energies of solvation of  $\text{M}^+\text{@C}_{60}$  are unknown; however, the calculated  $\Delta G_s$  values agree with the published data on hydration of bulky hydrophobic ions, *e.g.*,  $\text{PPh}_4^+$  and  $\text{AsPh}_4^+$ ,<sup>34</sup> as well as  $(n\text{-C}_3\text{H}_7)_4\text{N}^+$  and  $(n\text{-C}_5\text{H}_{11})_4\text{N}^+$ .<sup>35</sup>

Table 1 also lists the data characterizing the electron density distribution in  $\text{K}^+\text{@C}_{60}$ . The Mulliken atomic charges of  $\text{K}^+$ ,  $q_K(\text{Mull})$ , are scattered between 0.48 and 1.56. The largest variations of  $q_K(\text{Mull})$  were obtained with the 6-31+G(d) basis set augmented with diffuse orbitals. At the same time, calculations of the electron density for the natural orbitals  $q_K(\text{NAO})$ <sup>36</sup> in all cases predict a  $\text{K}^+$  charge of about 0.9, which corresponds to transfer of nearly 0.1e from the fullerene cage to the central metal ion.

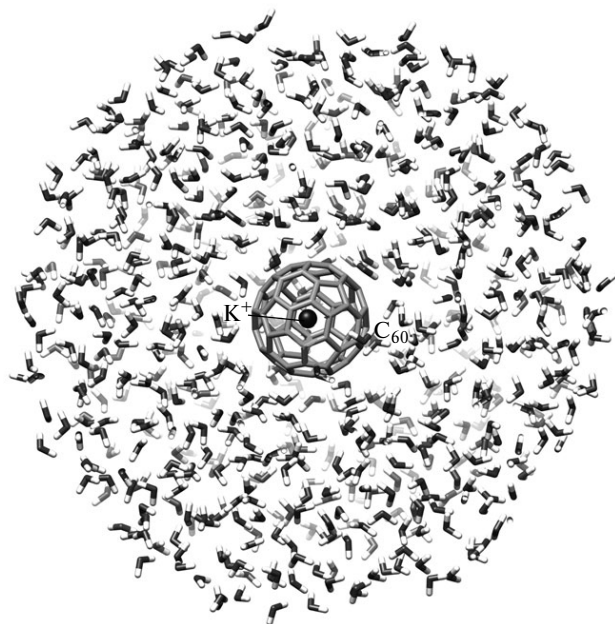
**Table 2.** Contributions to the Gibbs free energies of solvation  $\Delta G_s(\text{M}^+\text{@C}_{60})$  for the equilibrium positions of ions obtained from B3LYP/LANL2DZ/PCM calculations

Compound	$\Delta r_{\min}/\text{nm}$	$\Delta G_{\text{cav}}$ $-\Delta G_{\text{disp}}$ $\Delta G_{\text{rep}}$ $-\Delta G_{\text{s,el}}$ $-\Delta G_s$				
		kJ mol <sup>-1</sup>				
$\text{Li}^+\text{@C}_{60}$	0.14	187.3	172.8	9.7	162.2	137.9
$\text{K}^+\text{@C}_{60}$	0	187.3	174.6	9.7	159.9	137.5

The much weaker dependence of  $q(\text{NAO})$ , compared to  $q(\text{Mull})$ , on the computational method was reported for many systems.<sup>37</sup> For  $\text{K}^+\text{@C}_{60}$ , the best agreement between  $q(\text{Mull})$  and  $q(\text{NAO})$  was obtained from the B3PW91/LANL2DZ calculations (see Table 1). B3LYP/LANL2DZ calculations of the electron density in  $\text{Li}^+\text{@C}_{60}$  for the equilibrium  $\Delta r_{\min}$  value gave  $q_K(\text{Mull}) = 0.62$  and  $q_K(\text{NAO}) = 0.89$ ; no marked nonuniformity of the electron density distribution over the fullerene carbon atoms was revealed. By and large, the atomic charges in  $\text{Li}^+\text{@C}_{60}$  and  $\text{K}^+\text{@C}_{60}$  appeared to be close. The  $q(\text{NAO})$  charges were used in subsequent MD simulations using microscopic models for endohedral metallofullerenes.

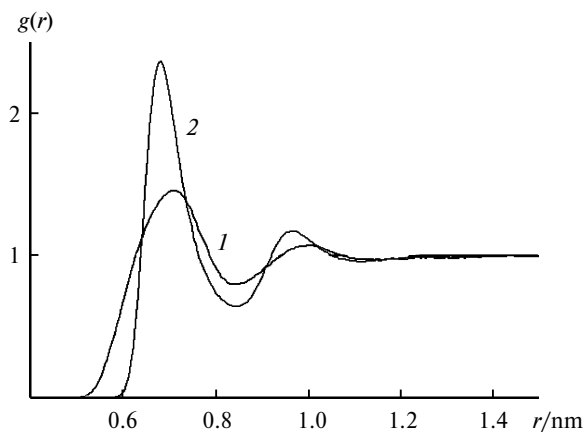
A limitation of the macroscopic description of hydration effects is the lack of information on the spatial distribution and polarization of water molecules surrounding the solute. To evaluate these effects, in the present work we studied the molecular dynamics of  $\text{K}^+$ ,  $\text{C}_{60}$ ,  $\text{Li}^+\text{@C}_{60}$ , and  $\text{K}^+\text{@C}_{60}$  for the microscopic model of a water sphere (Fig. 2) and calculated the corresponding RDF of water molecules.

The  $g_O(r)$  plots for the density of water O atoms (Fig. 3) show differences between the RDF for  $\text{Li}^+\text{@C}_{60}$  and  $\text{K}^+\text{@C}_{60}$ . In the former case, the calculated distribution exhibits a flat shoulder toward the central ion, which is due to the displacement of  $\text{Li}^+$  toward the inner surface of fullerene. However, maxima in both plots (see Fig. 3) are at nearly the same positions. A comparison of the  $g_O(r)$  and  $g_H(r)$  plots for the density of water (see Figs 3 and 4) shows that the RDF around the central ion of  $\text{M}^+\text{@C}_{60}$  are similar to the RDF of fullerene  $\text{C}_{60}$ . Transition from the idealized charge distribution to the  $q(\text{NAO})$  charges (*cf.* Figs 3 and 4) has little effect and manifests itself in the case of  $q(\text{NAO})$  as a somewhat longer shoulder in the RDF for the density of water and a somewhat more "fixed" orientation of water dipoles at short distances. The RDF calculated for  $\text{C}_{60}$  are in good agreement with the pub-

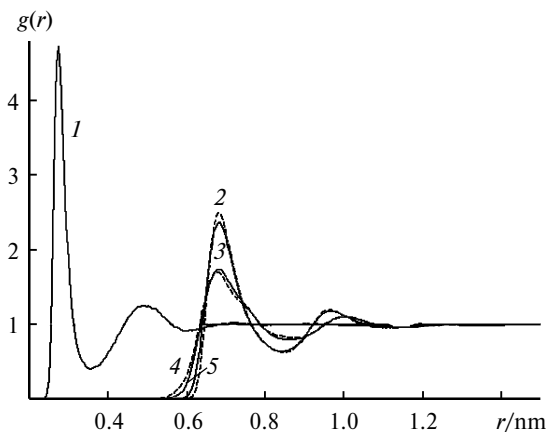


**Fig. 2.** Model for MD calculations: an endohedral metallofullerene surrounded by H<sub>2</sub>O molecules from a water sphere of radius 1.9 nm.

lished data<sup>19</sup> obtained for the "simple point charge" model of H<sub>2</sub>O and periodic boundary conditions. In regard to the effects of the charge of the metallofullerene, it should be noted that the  $g_O(r)$  RDF of the K<sup>+</sup> ion in solution (see Fig. 4) is close to unity at the distances corresponding to the first maximum of  $g_O(r)$  for C<sub>60</sub> and, therefore, the effect of the central ion in K<sup>+</sup>@C<sub>60</sub> on the density of water at the corresponding distances is rather weak. Nevertheless, the distributions  $f_\theta(r)$  of the average cosine of the orientation angle of the water dipole vector  $\vec{\mu}_w$  for C<sub>60</sub> and K<sup>+</sup>@C<sub>60</sub> are different (Fig. 5). The  $\langle \cos(\theta) \rangle$  values for C<sub>60</sub>



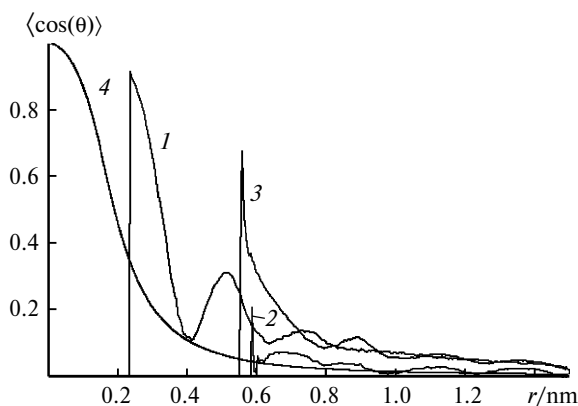
**Fig. 3.** The RDF of the density of water O atoms for Li<sup>+</sup>@C<sub>60</sub> (1) and K<sup>+</sup>@C<sub>60</sub> (2) plotted based on the MD trajectories depending on the distance to the central atom  $r$ . The charge on the central ion was set to +1.



**Fig. 4.** The RDF of the density of O (1–3) and H (4, 5) atoms of water for K<sup>+</sup> (1), C<sub>60</sub> (2, 4) and K<sup>+</sup>@C<sub>60</sub> (3, 5). Atomic charges in the endometallofullerene were chosen based on the  $q(\text{NAO})$  values obtained from DFT calculations.

are quite small at all distances from the center except a small peak in the zone of direct contact between water molecules and fullerene surface. For K<sup>+</sup>@C<sub>60</sub>, the  $f_\theta(r)$  peak in positions of direct contact with water is much higher than for C<sub>60</sub> due to the effect of the electric charge of the endohedral metallofullerene. The  $f_\theta(r)$  plots show that the orientational ordering of water molecules at the contact distances around K<sup>+</sup>@C<sub>60</sub> is higher than around K<sup>+</sup> at the same distances. Thus, the fullerene cage also to some extent affects the orientations of water molecules in the first hydration shell.

It is interesting to compare the analytical estimate of  $\langle \cos(\theta) \rangle$  obtained using the Langevin formula (see, e.g., Refs 34 and 38) with the  $g_O(r)$  values obtained from MD calculations. The Langevin formula gives an average cosine of the angle between a point dipole vector  $\vec{\mu}$  and the



**Fig. 5.** Average orientation of water dipoles  $\langle \cos(\theta) \rangle$  for K<sup>+</sup> (1), C<sub>60</sub> (2) and K<sup>+</sup>@C<sub>60</sub> (3) as a function of the distance to the central atom  $r$ . Atomic charges of the endohedral metallofullerene were chosen in accordance with the  $q(\text{NAO})$  values, the Langevin function (4) was calculated taking into account the distance-dependent water dipole shielding function.

effective electric field  $\vec{E}$  under thermal equilibrium conditions:

$$\langle \cos(\theta) \rangle = L(\beta\mu E) = \frac{\exp(\beta\mu E) + \exp(-\beta\mu E)}{\exp(\beta\mu E) - \exp(-\beta\mu E)} - \frac{1}{\beta\mu E}, \quad (1)$$

where  $\beta = 1/(kT)$ ,  $k$  is the Boltzmann constant, and  $T$  is absolute temperature (K). The energy of a point dipole  $\vec{\mu}$  in the field created by a point charge  $q$  depends on the distance  $r$  between them:

$$W(r) = -2.89q\vec{\mu}\vec{r}/r^3, \quad (2)$$

where  $W$  is expressed in  $\text{kJ mol}^{-1}$ ,  $\mu$  is expressed in D, and  $r$  is expressed in nm. For  $q = +1$ ,  $\mu_w(\text{TIP3P}) = 2.35$  D, and taking into account the distance-dependent shielding function of the electric field of the solvent  $\epsilon_w(r)$ ,<sup>38</sup> substitution of expression (2) to Eq. (1) gives an analytical dependence of  $\langle \cos(\theta) \rangle$  on  $r$  (see the plot in Fig. 5). In this case, the Langevin formula predicts a somewhat faster decrease in  $\langle \cos(\theta) \rangle$  at short  $r$  compared to the results of MD calculations. The difference can be due to the fact that the parameteric relation for  $\epsilon_w(r)$  was derived based on the calculations of the enthalpies of hydration within the framework of a continuum description of the solvent,<sup>38</sup> whereas the effective value of  $\epsilon_w(r)$  at short distances can be somewhat smaller for the model in which water molecules are specified explicitly. It should be noted that the  $f_\theta(r)$  curves calculated by molecular simulation have a wave-like shape in contrast to the smooth curve of the Langevin function.

Thus, our study showed that hydrophobic ions of endohedral metallofullerenes with encapsulated alkali metal cations are characterized by negative hydration energy, which may provide a rather high solubility of these systems in water. At the same time,  $\Delta G_s$  are low in absolute value; this reduces the permeability barrier through non-polar biomembranes. The endohedral metallofullerenes  $\text{Li}^+@\text{C}_{60}$  and  $\text{K}^+@\text{C}_{60}$  are characterized by close  $\Delta G_s$  values in spite of different equilibrium positions of the central ions. The fullerene carbon cage has a crucial effect on the RDF of the density of water molecules surrounding the charged endohedral metallofullerene. The influence of the positive charge of  $\text{M}^+@\text{C}_{60}$  is reduced to pronounced orientational effect on the  $\text{H}_2\text{O}$  molecules. Such properties of charged endohedral metallofullerenes can be important in the design of BACs based on them. Investigations of fullerene binding to biomolecules are planned for the future.

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